

## Analysis of equilibrium states in a Pople-Karasz model using mean and Gaussian curvatures

In earlier works on Pople-Karasz model [1, 2], equilibrium states are displayed by contour mapping, where one coordinate is associated with the orientational order parameter  $S$  and the other with the positional order parameter  $Q$ . In this work, we introduce their geometric analysis by determining mean and Gaussian curvatures ( $H, K$ ). From the temperature variation of  $H$  and  $K$  in the disordered state ( $S = Q = 1/2$ ), we have reported the local shapes of equilibrium free energies for the stable and unstable solutions. It is important to mention that a minimal surface for the disordered case with  $H = 0, K < 0$  is explicitly observed. For the ordered case ( $S > 1/2, Q > 1/2$ ), it is found that the curvature  $H$  displays a cusp singularity and a convergence of  $K$  is observed at the criticality. These results are compared with the similar works [3] and a very good agreement is found.

[1] M. Keskin, Ş. Özgan, A Model for Studying How to Obtain the Metastable States, *Physica Scripta* 42 (1990) 349-354.

[2] Ş. Özgan, Investigation of stable, metastable and unstable solutions on molecular crystals, *Mod. Phys. Lett. B* 21 (2007) 817-830.

[3] R. Erdem, Mean and Gaussian curvatures of equilibrium states for a spin-1 Ising system: existence of minimal surface in the paramagnetic solutions, *Eur. Phys. J. Plus* 138 (2023) 306.

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