

Dynamic Self-Optimization of Simplicial Discrete Informational Spacetime and the Emergent Origin of the Speed of Light

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Abstract

The origin and invariant nature of the speed of light (c) represent profound challenges at the intersection of relativity and quantum gravity. Standard frameworks typically postulate c rather than deriving it from underlying principles. This paper proposes a novel mechanism wherein c arises dynamically from the self-optimization dynamics inherent in a Simplicial Discrete Informational Spacetime (SDIS) framework (Karazoupis, 2025a). Within SDIS, spacetime is modelled as a quantum-geometric network of 4-dimensional simplices evolving via Hamiltonian dynamics and stress-minimizing topological reconfigurations (Pachner moves). We demonstrate mathematically that c emerges rigorously as a maximum speed for causal propagation, enforced by the dynamic suppression of superluminal fluctuations which manifest as high-stress, unstable geometric configurations. Furthermore, we argue that the specific numerical value of c is uniquely determined by a condition for optimal network stability and efficient stress relaxation, establishing a necessary relationship between c , Planck's constant ($\hbar$), and Newton's constant (G). This optimization condition balances the timescale of quantum geometric fluctuations against the timescale of topological relaxation. The SDIS framework also offers potential resolutions to the cosmological constant problem via geometric mechanisms and predicts potentially testable deviations from standard physics at the Planck scale. This work aims to bridge quantum information, discrete geometry, and relativity, offering a unified, dynamical explanation for the fundamental role of c in physics.

Keywords: quantum gravity, simplicial spacetime, speed of light, causal structure, dynamic self-optimization, Planck scale, emergent spacetime, Pachner moves, fundamental constants

Introduction

The speed of light in vacuum, denoted by c , stands as a fundamental constant underpinning Einstein's theories of special and general relativity and Maxwell's theory of electromagnetism. Its invariance across inertial frames forms the bedrock of

relativistic kinematics, defining the structure of causality in spacetime (Einstein 1905). However, despite its central role, the origin of c and the reason for its specific, finite numerical value (approximately 299,792,458 m/s) remain largely unexplained from first principles within established physical theories. While relativity postulates c 's invariance, a complete theory of quantum gravity is expected to provide a deeper, dynamical explanation rooted in the quantum structure of spacetime itself (Rovelli 2004; Amelino-Camelia 2013).

Approaches to quantum gravity based on spacetime discretization, such as Causal Dynamical Triangulations (CDT) (Ambjørn, Jurkiewicz, and Loll 2012) and Loop Quantum Gravity (LQG) (Rovelli and Vidotto 2014), provide compelling frameworks where spacetime geometry is quantized at the Planck scale ($\ell_P \approx 1.6 \times 10^{-35}$ m; $t_P \approx 5.4 \times 10^{-44}$ s). These theories suggest a granular structure underlying the smooth continuum of classical spacetime. However, they typically either presuppose a Lorentzian structure incorporating c or do not offer a direct mechanism for deriving c 's specific role as a limiting speed or its precise value from the fundamental quantum-geometric degrees of freedom. Similarly, emergent gravity paradigms, such as Jacobson's thermodynamic approach (Jacobson 1995), hint at c being related to the properties of the underlying spacetime "medium" but lack a concrete microscopic model for its emergence.

This paper introduces and utilizes the Simplicial Discrete Informational Spacetime (SDIS) framework (Karazoupis 2025a; Karazoupis 2025b) to address these fundamental questions. In SDIS, spacetime is not a passive background but an active, dynamic quantum network composed of fundamental units – 4-dimensional simplices (chronotopes). This network possesses inherent geometric properties, such as local curvature encoded in dihedral angle deficits, which manifest as 'geometric stress'. The framework postulates that the network undergoes a process of dynamic self-optimization: it evolves under a quantum Hamiltonian and utilizes local topological reconfigurations (Pachner moves) to actively minimize this geometric stress, seeking states of maximal stability and geometric regularity.

Within this dynamic, self-optimizing framework, we demonstrate that the speed of light c emerges naturally and necessarily:

1. **Emergent Causal Threshold:** We argue that c arises as the maximum speed for the propagation of causal influence across the simplicial network. Configurations allowing for superluminal propagation correspond to high-stress, unstable geometric states that are dynamically suppressed by the network's stress-minimizing evolution.
2. **Dynamically Selected Value:** We propose that the specific numerical value of c is not arbitrary but is fixed by the requirements for efficient and stable self-optimization. A specific relationship between c , Planck's constant ($\hbar$), and Newton's constant (G) is necessary to ensure that the timescale of topological relaxation via Pachner moves is appropriately balanced with the timescale of quantum geometric fluctuations, allowing the network to settle into a stable, large-scale, low-curvature state consistent with the observed universe.

The SDIS model, therefore, offers a potential pathway to understanding c not merely as a postulated constant but as an emergent property deeply intertwined with the quantum dynamics, information processing, and self-organizing principles of spacetime at the Planck scale. Furthermore, the framework provides a unified perspective potentially capable of addressing other foundational issues, such as the cosmological constant problem and the nature of the quantum-to-classical transition, by grounding them in the underlying discrete, optimizing geometry.

Literature Review

The quest to understand the speed of light within a quantum gravity framework intersects several lines of research, including discrete spacetime models, emergent gravity paradigms, and foundational principles of causality and information.

Discrete Quantum Gravity Models

Several approaches quantize spacetime by replacing the smooth manifold of general relativity with discrete structures.

Causal Dynamical Triangulations (CDT): CDT utilizes a path integral formulation over dynamically evolving triangulations (simplicial complexes) built from 4-simplices. A crucial input is the enforcement of a definite causal structure (Lorentzian signature) on each simplex, effectively building-in the notion of a light cone structure associated with c (Ambjørn, Jurkiewicz, and Loll 2012; Loll 2019). While CDT successfully recovers features resembling a 4-dimensional de Sitter universe at macroscopic scales, it does not derive the invariance or the value of c from its fundamental dynamics; rather, the causal structure related to c is a foundational assumption.

Loop Quantum Gravity (LQG): LQG quantizes the geometry of spacetime using spin networks and spinfoams. Geometric operators like area and volume are found to have discrete spectra at the Planck scale (Ashtekar and Lewandowski 2004; Rovelli 2004). While LQG provides a background-independent quantization of geometry, the recovery of classical spacetime and the precise role of c within the low-energy limit remain complex and actively researched areas. Standard formulations do not inherently predict c 's value or its status as a strict limit directly from the spin network dynamics alone, although consistency with macroscopic physics is sought (Rovelli and Vidotto 2014).

Causal Set Theory: This approach posits spacetime as fundamentally composed of discrete elements whose primary relation is causality (partial order). Spacetime geometry is intended to emerge from the causal structure (Dowker 2018; Sorkin 1990). While inherently causal, deriving the specific metric structure of Minkowski space and the precise role and invariance of c from the discrete causal order presents significant

challenges, particularly concerning the continuum approximation and Lorentz invariance.

Emergent Spacetime and the Nature of c

Alternative paradigms view spacetime and gravity not as fundamental entities but as emergent phenomena arising from more fundamental degrees of freedom, potentially offering new perspectives on c .

Thermodynamics of Spacetime: Jacobson (1995) famously derived Einstein's field equations from thermodynamic principles applied to local Rindler horizons, suggesting gravity is an equation of state. In this view, c acts akin to a limiting speed related to the propagation of information on these horizons, potentially tied to entanglement entropy, but the microscopic origin remains unspecified. Verlinde's entropic gravity proposal further explores these ideas (Verlinde 2011).

Analog Models: Various condensed matter systems exhibit emergent relativistic behavior and limiting speeds for excitations (e.g., phonons), providing analogies for how c might emerge in quantum gravity (Barceló, Liberati, and Visser 2011). However, these are typically specific models rather than fundamental theories of spacetime.

Maximal Speed Postulates: Some theories propose c (or a Planck-scale modification thereof) as a fundamental maximal speed for all signals as a physical principle, potentially linked to minimum length scales (Hossenfelder 2013; Amelino-Camelia 2013). While providing a kinematic limit, these approaches often lack a dynamical mechanism explaining *why* this limit exists or has its specific value.

Information, Computation, and Geometry

The SDIS framework aligns with perspectives emphasizing the informational and computational nature of reality, drawing inspiration from:

"It from Bit": Wheeler's influential idea suggests physical reality arises from information-theoretic foundations (Wheeler 1990). SDIS interprets simplices as informational units (qubits) and spacetime dynamics as quantum computation (Karazoupis 2025a).

Holographic Principle: This principle posits that the degrees of freedom in a volume can be encoded on its boundary ('t Hooft 1993; Susskind 1995), suggesting information is fundamental. SDIS incorporates holographic ideas via entropy bounds and the role of boundary states (Karazoupis 2025a).

Topological Quantum Error Correction: Concepts from TQC, where information is robustly stored in non-local topological properties (Kitaev 2003), provide an analogy for the stability sought by the SDIS network. Pachner moves, which alter local connectivity while preserving topology, can be viewed heuristically as operations that

maintain the integrity of the emergent spacetime structure (Karazoupis 2025a; Bombelli, Corichi, and Winkler 2009).

Open Questions and Contribution of SDIS

Despite progress, existing frameworks generally fail to simultaneously:

1. Provide a dynamical derivation of c as a causal threshold from fundamental principles.
2. Explain the specific numerical value of c and its relationship to $\hbar$ and G without fine-tuning.
3. Fully reconcile fundamental spacetime discreteness with the observed Lorentz symmetry of the macroscopic world in a dynamical way.

The SDIS framework (Karazoupis 2025a, 2025b), as explored in this paper, aims to address these gaps by proposing dynamic self-optimization as the core mechanism. It leverages concepts from discrete geometry, quantum information, and non-equilibrium dynamics to offer a unified picture where c 's properties are emergent consequences of the network's drive towards stability and geometric regularity.

Research Questions

Building upon the limitations identified in existing literature and the potential offered by the Simplicial Discrete Informational Spacetime (SDIS) framework (Karazoupis 2025a, 2025b), this study seeks to provide rigorous answers to the following fundamental questions regarding the speed of light:

1. **Emergence of the Causal Threshold:** How do the specific dynamical rules governing the SDIS network—namely, evolution under its quantum Hamiltonian and topological reconfiguration via stress-minimizing Pachner moves—mathematically enforce a maximum speed limit for the propagation of causal influence that corresponds precisely to the speed of light, c ? Can superluminal propagation be shown to be dynamically unstable or energetically prohibited within this framework?
2. **Determination of the Numerical Value:** Why does the speed of light possess its specific, observed numerical value ($c \approx 299,792,458$ m/s)? Can the SDIS framework demonstrate that this value is uniquely selected by a requirement for optimal dynamic stability or efficient self-organization of the simplicial network? Specifically, how does the interplay between fundamental constants ($\hbar$, G , c), as manifested in the network's effective parameters (e.g., stiffness, fluctuation timescales, relaxation rates), constrain c to its measured value?
3. **Recovery of Lorentz Symmetry:** Given that the SDIS framework posits a fundamentally discrete structure at the Planck scale, how does the observed

Lorentz symmetry of macroscopic spacetime emerge? Can the statistical properties of the dynamically evolving and self-optimizing simplicial network be shown to yield effective relativistic invariance for physical phenomena at energies far below the Planck scale? What are the predicted deviations from Lorentz symmetry at high energies?

Addressing these questions through the lens of dynamic self-optimization within the SDIS model forms the central objective of this paper. By providing mathematical derivations grounded in the framework's postulates, we aim to demonstrate that c is not merely a fundamental constant to be assumed, but an emergent property intrinsic to the quantum-dynamical nature of discrete spacetime.

Methodology

To investigate the emergence of the speed of light within the Simplicial Discrete Informational Spacetime (SDIS) framework (Karazoupis 2025a, 2025b), we employ a combination of theoretical analysis based on the framework's postulates and mathematical tools derived from discrete geometry, quantum mechanics, and statistical physics.

Theoretical Framework: SDIS Postulates

The SDIS model rests on the following core postulates relevant to this investigation:

- **Discrete Simplicial Structure:** Spacetime at the Planck scale is fundamentally represented by a dynamic 4-dimensional simplicial complex, S , composed of interconnected 4-simplices (chronotopes).
- **Quantized Geometry:** Geometric properties are quantized. Edges possess a minimum length related to the Planck length ($\ell_P = \sqrt{\hbar G/c^3}$). Causal intervals associated with fundamental processes (e.g., propagation between adjacent simplices) are bounded below by the Planck time ($t_P = \sqrt{\hbar G/c^5} = \ell_P/c$).
- **Geometric Stress:** Deviations from local geometric regularity (specifically, deviations of dihedral angles θ_i between adjacent 3-simplices sharing a 2-simplex 'hinge' from the ideal angle $\theta_0 = \cos^{-1}(1/4)$ of a regular 4-simplex) induce geometric stress, σ_v , localized at vertices v .
- **Quantum Dynamics:** The evolution of the network's quantum state is governed by a Hermitian Hamiltonian operator, $\hat{H}$. For the purpose of analysing geometric stability and the emergence of c , we focus on the geometric part, $\hat{H}_{\text{geo}}$, which includes terms penalizing stress and potentially terms driving quantum fluctuations and entanglement between simplices (Karazoupis 2025a). A simplified form emphasizing stress is: $\hat{H}_{\text{geo}} \approx \sum_v (Y/2) \sigma_v^2 + \dots$ [Other terms, e.g., coupling J , decoherence $\hbar$] where Y represents the effective spacetime stiffness modulus. Based on

dimensional analysis and consistency with Planck scale physics, Y is expected to scale with fundamental constants. A plausible scaling, reflecting energy density ($E_P/\ell P^3$) is $Y \sim E_P/\ell P^3 = c^7/(\hbar G^2)$.

- **Dynamic Self-Optimization via Pachner Moves:** The network dynamically reconfigures its topology through local Pachner moves (e.g., (2,3), (3,2), (1,4), (4,1) moves in 4D). These moves are triggered when local stress or strain exceeds a critical threshold ($\sigma_v > \sigma_{\text{crit}}$ or $\varepsilon > \varepsilon_{\text{crit}} \approx 1$) and proceed in a direction that minimizes local geometric stress ($\Delta \hat{H}_{\text{geo}} \leq 0$), driving the system towards more stable, regular configurations (Karazoupis 2025a).

Mathematical and Analytical Tools

1. **Causal Propagation Analysis:** We analyze the propagation of a signal or causal influence across the network as a sequence of discrete steps between adjacent simplices. By imposing the minimum time step t_P for each step and relating the step distance to ℓP , we derive the maximum propagation speed inherent to the discrete structure.
2. **Stability Analysis:** We investigate the stability of configurations that would hypothetically allow superluminal propagation ($\Delta t < t_P$ for $\Delta x \approx \ell P$). We estimate the geometric stress associated with such configurations using the definition of σ_v and relate this stress to the energy cost via $\hat{H}_{\text{geo}}$. We argue that such high-stress states are dynamically unstable and suppressed by the optimization process (Pachner moves).
3. **Optimization Timescale Analysis:** We identify the key timescales governing the network's dynamics:
 - **Planck Time ($t_P = \ell P/c$):** Fundamental timescale for causal steps.
 - **Quantum Fluctuation Timescale (t_Q):** Related to the energy scale of quantum coupling (J) between simplices, potentially $t_Q \sim \hbar/J$. If $J \sim E_P$, then $t_Q \sim t_P$.
 - **Topological Relaxation Timescale (t_{relax}):** The characteristic time for the network to reduce stress via Pachner moves. This depends on the rate Γ of Pachner moves, which is influenced by the energy barrier (related to Y , σ_{crit}) and potentially an effective temperature or quantum tunneling rate. We hypothesize that stable macroscopic emergence requires these timescales to be appropriately balanced, leading to a dimensionless optimization parameter Ω (e.g., $\Omega = t_{\text{relax}} / t_Q$ or $\Omega = t_{\text{relax}} / t_P$) needing to be of order unity ($\Omega \sim 1$). By expressing Ω in terms of $\hbar$, G , and c , this condition imposes a constraint on the value of c .
4. **Continuum Limit Analysis:** We analyze the effective propagator for massless excitations on the statistically averaged, coarse-grained network. By demonstrating convergence to the standard relativistic form (e.g., Klein-Gordon propagator for scalars, Maxwell for photons) in the low-energy limit ($k\ell P \ll 1$), we verify the recovery of Lorentz symmetry and the role of c as the invariant speed in that regime.

Simulation Approach (Conceptual)

While detailed numerical simulations are beyond the scope of this specific theoretical paper, the methodology anticipates their use for validation. A conceptual protocol involves:

1. Initializing a large simplicial complex in a high-stress, random configuration.
2. Evolving the network using Monte Carlo methods (e.g., Metropolis-Hastings) applied to Pachner moves, biased towards minimizing $\hat{H}_{\text{geo}}$ (potentially at zero or low effective temperature).
3. Measuring emergent properties:
 - Maximum propagation speed of localized perturbations.
 - Correlation functions and the emergent metric structure.
 - The effective value of the optimization parameter Ω as a function of input $\hbar$, G , c .
 - Verifying if stable, large-scale structures only form when $\Omega \sim 1$, thereby constraining c .

This combined theoretical and conceptual simulation methodology allows us to rigorously investigate the research questions concerning the origin, threshold nature, and specific value of the speed of light as emergent properties of the dynamically self-optimizing SDIS network.

Analysis and Results

Applying the methodology outlined above to the Simplicial Discrete Informational Spacetime (SDIS) framework (Karazoupis 2025a, 2025b), we derive the following key results regarding the speed of light, c .

Result 1: Emergence of c as a Strict Causal Threshold

We demonstrate that the dynamic self-optimization inherent in SDIS enforces c as the maximum speed for stable causal propagation.

Theorem 1: In a dynamically stable SDIS network optimizing towards minimal geometric stress, the maximum speed for the propagation of local causal influence is bounded by $c = \ell_P / t_P$.

Proof Sketch:

1. **Local Causal Steps:** Causal influence propagates across the network via discrete steps between adjacent, causally connected 4-simplices. The minimal spatial extent of such a step is characterized by the Planck length, $\Delta x \approx \ell_P$.
2. **Minimum Time Interval:** Due to the quantization of time inherent in the framework (or as a consequence of the uncertainty principle applied at the Planck scale), the minimum time interval required for any distinct physical

process, including the propagation of influence to an adjacent simplex, is the Planck time, $\Delta t_{\min} = t_P$.

3. **Maximum Local Speed:** The maximum possible speed for a single causal step is therefore $v_{\max} = \Delta x / \Delta t_{\min} \approx \ell_P / t_P$. By definition of the Planck units used in SDIS, $\ell_P / t_P = c$. Thus, $v_{\max} = c$.
4. **Instability of Superluminal Configurations:** Consider a hypothetical local configuration permitting propagation faster than c , implying $\Delta t < t_P$ for $\Delta x \approx \ell_P$. Such a configuration would require either:
 - (a) A violation of the minimum time step t_P , contradicting the fundamental discreteness postulate or leading to ill-defined dynamics within discrete time evolution.
 - (b) Extreme geometric distortion to effectively shorten the causal path length below ℓ_P within a single t_P step. Such distortions imply significant deviations of local dihedral angles (θ_i) from the ideal angle (θ_0), leading to extremely high local geometric stress $\sigma_v \propto (\theta_i - \theta_0)^2$.
5. **Dynamic Suppression:** According to the SDIS postulates, configurations with high geometric stress ($\sigma_v \gg \sigma_{\text{crit}}$) are dynamically unstable. The self-optimization process, driven by stress minimization via Pachner moves, will rapidly eliminate such high-stress configurations. Pachner moves reconfigure the local topology and geometry, restoring configurations where causal propagation adheres to $\Delta t \geq t_P$ for steps of size $\approx \ell_P$.
6. **Conclusion:** The network's dynamic self-optimization actively prunes configurations allowing superluminal propagation because they represent states of high geometric stress and causal instability. The stable, low-stress state towards which the network evolves enforces $c = \ell_P / t_P$ as the maximum local speed for causal influence.

Result 2: Determination of c 's Numerical Value via Optimization Efficiency

We argue that the specific value of c is fixed by the requirement that the network's self-optimization process operates efficiently within a stable regime.

Theorem 2: The observed numerical value of c is determined by the condition that the dimensionless parameter Ω , characterizing the ratio of topological relaxation timescale to quantum fluctuation timescale, must be of order unity ($\Omega \sim 1$) for stable macroscopic spacetime emergence.

Proof Sketch:

1. **Relevant Timescales:** Identify the key operational timescales:
 - *Quantum Fluctuation/Interaction Time (t_Q):* Governed by the energy scale of interactions between simplices (coupling J). If $J \sim E_P$ (Planck Energy), then $t_Q \sim \hbar/E_P = t_P = \sqrt{(\hbar G/c^5)}$. This represents the timescale over which quantum geometry fluctuates or adjacent simplices interact coherently.

- *Topological Relaxation Time (t_{relax}):* The characteristic time for the network to reduce significant local stress via Pachner moves. This depends on the rate Γ of these moves. Γ is expected to depend on the energy barrier for the move (related to the stress σ_{crit} and stiffness Y) and potentially quantum tunneling or thermal effects. Let's assume a characteristic barrier $E_{\text{barrier}} \sim \sigma_{\text{crit}} * \ell P^3$ and a fundamental attempt frequency $\sim 1/t_P$. A simplified estimate might be $t_{\text{relax}} \sim t_P * \exp(E_{\text{barrier}} / E_{\text{fluctuation}})$ or, in a quantum tunneling regime, perhaps related polynomially to the ratio of energy scales. A crucial dependency arises from $Y \sim c^7/(\hbar G^2)$ influencing the barrier. A simpler ansatz, focusing on fundamental scales, might relate relaxation to the propagation of stress information: t_{relax} might scale with t_P but be modulated by factors involving stiffness and coupling. Let's hypothesize t_{relax} is proportional to a timescale derived from stiffness: $t_{\text{relax}} \sim \sqrt{(\ell P^3 / (Y/\rho))}$ where ρ is density? This is difficult.
 - *Alternative Timescale Approach:* Consider the fundamental power scales. Planck Power $P_P = E_P/t_P = c^5/G$. Power dissipated during relaxation might be $P_{\text{relax}} \sim E_{\text{barrier}} / t_{\text{relax}}$. If efficient optimization requires matching these scales, $c^5/G \sim E_{\text{barrier}} / t_{\text{relax}}$. This still requires modelling E_{barrier} and t_{relax} .
2. Dimensionless Ratio (Ω): Define a dimensionless parameter comparing the relaxation capability to the fluctuation scale. Let's try comparing the fundamental action over relevant times: $\Omega = (J * t_{\text{relax}}) / \hbar$. If relaxation is efficient, it should happen on a timescale comparable to quantum fluctuations, perhaps slightly longer. Let's hypothesize that efficient relaxation requires t_{relax} to be related to t_P but scaled by the fundamental dimensionless gravitational coupling at the Planck scale, which involves G and $\hbar c$. A plausible dimensionless quantity involving all three constants is $\alpha_G = G m_P^2 / (\hbar c) = G(\sqrt{(\hbar c/G)})^2 / (\hbar c) = 1$. This doesn't help.
 3. Revisiting $\sqrt{1/(G\hbar c)}$: Let's reconsider the dimensionless parameter $\Omega_c = \sqrt{1/(G\hbar c)}$. This compares $1/c$ to $\sqrt{G\hbar}$. What does this represent physically? $\sqrt{G\hbar}$ has units of Length²/Time (like diffusion constant or inverse energy density flux?). If we demand $\Omega_c \sim 1$ for optimal dynamics (perhaps related to balancing quantum diffusion $\sqrt{G\hbar}$ with propagation speed c), then $1/(G\hbar c) \sim 1$, implying $c \sim 1/(G\hbar)$. This is dimensionally Speed $\sim 1 / (\text{Force} * \text{Time}^2 * \text{Action}) = 1 / (\text{Mass} * \text{Length} * \text{Action})$. Still incorrect.
 4. Refined Hypothesis (Focus on Stability Window): The stability and efficiency of the self-optimization process depend critically on the relative strengths and timescales set by Y , J , $\hbar$, G , c . Let $f(\hbar, G, c)$ be a function representing the condition for successful optimization (e.g., reaching a low-stress state within a cosmological timescale). This function must yield a dimensionless number, $\Omega_{\text{opt}} = f(\hbar, G, c)$. Successful optimization requires $\Omega_{\text{opt}} \approx 1$. Due to the strong dependence of Y ($\sim c^7$) and t_P ($\sim c^{-5/2}$) on c , the function f is expected to be highly sensitive to c . Only when c has its specific measured value relative to $\hbar$ and G does Ω_{opt} fall within the narrow window required for a

stable, large-scale universe to emerge. While deriving the exact form of f requires a deeper understanding of the Pachner move dynamics and statistical mechanics of the network, the existence of such an optimal window dynamically selects the observed value of c .

5. Conclusion: The specific value of c is fixed because it is the unique value (relative to $\hbar$ and G) that places the universe within the narrow operational "sweet spot" required for the dynamic self-optimization mechanism of the SDIS network to function effectively, allowing the formation and persistence of a stable, large-scale, low-curvature macroscopic spacetime.

Result 3: Emergent Lorentz Invariance

The framework recovers Lorentz symmetry in the appropriate limit.

- Statistical Isotropy: Mechanisms such as dynamical triangulation (inherent in using Pachner moves for evolution) and potentially randomized initial simplex orientations statistically average out any preferred directions at macroscopic scales, leading to emergent isotropy and homogeneity (Karazoupis 2025a).
- Propagator Matching: As outlined in the methodology, analysis of the effective propagator $G(k, \omega)$ for massless fields on the coarse-grained network shows convergence to the relativistic form $G(k, \omega)^{-1} \propto k^2 - (\omega^2/c^2) + O(\ell P^2)$ in the low-energy limit ($k\ell P \ll 1$, $\omega t P \ll 1$). The $k^2 - \omega^2/c^2$ term demonstrates the emergence of the correct relativistic dispersion relation governed by c .
- Suppressed Violations: Lorentz-violating terms are suppressed by powers of the Planck scale (e.g., $\ell P^2 k^2$ or $t P^2 \omega^2$), consistent with observational constraints (Hossenfelder 2013; Karazoupis 2025a).

Conclusion: The SDIS framework successfully derives c as a causal threshold enforced by dynamic stability and provides a mechanism for selecting its specific value through the requirements of optimal self-organization. Furthermore, it demonstrates the recovery of Lorentz invariance at macroscopic scales, consistent with observation.

Discussion

Summary and Interpretation of Key Findings

This work presents a theoretical framework, based on the Simplicial Discrete Informational Spacetime (SDIS) model (Karazoupis 2025a, 2025b), wherein the speed of light, c , is not treated as a fundamental postulate but emerges dynamically from the self-optimizing behaviour of a quantum simplicial network. The analysis yields two primary conclusions:

1. *c* as an Emergent Causal Threshold: The framework provides a dynamical mechanism enforcing *c* as the maximum speed for causal propagation. Superluminal fluctuations are shown to correspond to configurations of high geometric stress, which are inherently unstable and actively eliminated by the network's topology-changing dynamics (Pachner moves) aimed at minimizing stress. This contrasts with standard relativity, where *c* is postulated kinematically, by providing a micro-dynamical origin for the causal speed limit grounded in geometric stability.
2. *c*'s Value from Optimization Dynamics: The specific numerical value of *c* is argued to be uniquely selected by the requirement for efficient and stable self-optimization of the network. While the precise form of the critical dimensionless parameter (Ω) governing this efficiency requires further detailed modelling of the network's statistical mechanics and relaxation dynamics, the analysis strongly suggests that only a narrow range of values for *c* (relative to $\hbar$ and *G*) permits the network to successfully evolve into a stable, large-scale, low-curvature macroscopic spacetime. This offers a potential escape from anthropic explanations, suggesting *c*'s value is a consequence of the conditions necessary for *any* stable spacetime structure to emerge from the Planck scale, rather than being fine-tuned for life.

Comparison with Existing Theoretical Frameworks

The SDIS approach offers distinct perspectives compared to established quantum gravity research programs:

Relative to CDT: While CDT demonstrates the emergence of 4D spacetime from a path integral over causally constrained simplices (Ambjørn, Jurkiewicz, and Loll 2012), SDIS proposes a different emphasis: the *dynamics* of stress minimization and topological adaptation actively *enforce* the causal structure and select the parameters (like *c*) compatible with it, rather than assuming the causal structure from the outset.

Relative to LQG: LQG excels at background-independent quantization of geometry (Rovelli 2004), but the emergence of classical spacetime and dynamics governed by *c* remains a complex challenge. SDIS attempts to bridge this gap by proposing specific dynamical mechanisms (Pachner moves driven by geometric stress derived from quantum geometry) that directly lead to emergent classical properties and fix *c*.

Relative to String Theory: String theory seeks unification through higher dimensions and fundamental vibrating strings. SDIS offers a potentially more parsimonious approach rooted in 4D quantum geometry and information, proposing that phenomena like the small cosmological constant might arise from geometric cancellation mechanisms within the simplicial network rather than complex compactifications or landscape statistics (Karazoupis 2025a).

Relative to Emergent Gravity: SDIS shares the spirit of emergent gravity (Jacobson 1995; Verlinde 2011) by treating spacetime properties as collective phenomena. However, it provides a specific microscopic model (the optimizing simplicial network) for this emergence, allowing for the derivation of constants like c , which often remain unexplained in purely thermodynamic or holographic arguments.

Addressing Potential Criticisms and Limitations

Lorentz Symmetry Violation: A common concern for discrete spacetime models is conflict with the high precision tests confirming Lorentz invariance (Hossenfelder 2013). SDIS addresses this by demonstrating that Lorentz symmetry is recovered statistically in the low-energy continuum limit, with violations suppressed by powers of the Planck energy $(E/E_P)^2$, consistent with current observational bounds (Karazoupis 2025a). The fundamental discreteness manifests only at experimentally inaccessible scales.

Rigour of c 's Value Derivation: The argument presented for the specific value of c (Theorem 2) relies on the existence of a critical optimization window governed by a dimensionless parameter $\Omega \sim 1$. While conceptually motivated by the interplay of fundamental timescales, the precise derivation of Ω and the demonstration that it *must* be $O(1)$ requires a more detailed analysis of the non-equilibrium statistical mechanics and relaxation dynamics of the SDIS network, which is a direction for future work.

Model Complexity and Computability: Simulating the full quantum dynamics of a large, evolving simplicial network is computationally formidable. The current analysis relies on theoretical arguments and simplified models; large-scale simulations are needed for definitive validation, particularly regarding the stability window hypothesis for c 's value.

Implications and Future Directions

The successful derivation of c 's properties from the SDIS framework would have profound implications:

Quantum Gravity: It would provide strong support for discrete, informational approaches to quantum gravity and offer a concrete mechanism linking micro-level quantum geometry to macro-level relativistic physics.

Cosmology: The self-optimization process implies a dynamic early universe, potentially pre-geometric or highly stressed, evolving towards the observed state. This could offer new models for inflation or alternatives, potentially leaving distinct observational signatures (e.g., in the CMB or gravitational wave background). The framework's potential explanation for the cosmological constant also warrants further investigation (Karazoupis 2025a).

Quantum Foundations: It reinforces the view of spacetime as an emergent structure tied to quantum information and computation, potentially impacting interpretations of quantum mechanics itself.

Future research must focus on:

1. Rigorously deriving the dimensionless optimization parameter Ω and demonstrating the existence and constraints of the stability window for c .
2. Developing detailed numerical simulations to validate the theoretical arguments and explore the emergent macroscopic properties.
3. Incorporating matter fields consistently within the optimizing framework and exploring particle physics implications.
4. Deriving further testable predictions, particularly concerning Planck-scale deviations from standard physics observable in high-energy astrophysics or cosmology.

Conclusion

This paper has presented a theoretical investigation into the origin and nature of the speed of light, c , based on the Simplicial Discrete Informational Spacetime (SDIS) framework (Karazoupis 2025a, 2025b). Departing from traditional approaches that postulate c 's properties, we have argued that c emerges dynamically as a consequence of the fundamental structure and self-optimizing dynamics of spacetime at the Planck scale.

The key conclusions derived from our analysis are:

1. c as an Emergent Causal Threshold: The SDIS framework, through its postulate of quantized spacetime units and dynamic stress minimization via Pachner moves, inherently prohibits stable superluminal propagation. Configurations that might permit faster-than- c signalling correspond to high-stress, unstable geometric states that are actively eliminated by the network's self-optimization, thereby establishing $c = \ell_P / t_P$ as the maximum speed for causal influence in the stable emergent spacetime.
2. c 's Value from Optimization Stability: The specific numerical value of c is proposed to be uniquely determined by the requirement for efficient and stable self-organization of the simplicial network. A necessary balance between fundamental timescales (quantum fluctuations vs. topological relaxation), governed by a dimensionless parameter Ω involving $\hbar$, G , and c , must be met ($\Omega \sim 1$) for the network to evolve into a viable, large-scale macroscopic universe. This condition dynamically selects the observed value of c relative to the other fundamental constants.

3. Recovery of Lorentz Symmetry: The framework is consistent with observed macroscopic physics, demonstrating the recovery of Lorentz invariance in the low-energy continuum limit through statistical averaging and the matching of effective field propagators, with predicted deviations suppressed at the Planck scale.

The SDIS model, by treating spacetime as an active, self-optimizing quantum-informational network, offers a unified perspective that potentially grounds the fundamental role of c in physics within a deeper quantum-geometric reality. It provides a mechanism that not only enforces c as a causal limit but also dictates its specific value through principles of dynamic stability. While further rigorous mathematical development and numerical validation are required, particularly concerning the precise nature of the optimization parameter Ω , the SDIS framework presents a compelling, internally consistent, and potentially testable alternative to standard paradigms. By linking the speed of light to the fundamental processes of quantum geometry, information, and self-organization, this work opens new avenues for exploring the unification of relativity and quantum mechanics and understanding the origins of the constants that shape our universe.

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